


PV Performance Modeling with PVfit

Workflows that balance cost, complexity, and accuracy.

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Agenda

PVfit's Approach to Photovoltaic Modeling

2021 Blind PV Modeling Comparison

PV-Based Sensing and Other Opportunities

PVfit's Single-Diode Model (SDM)

6-parameter SDM for photovoltaic (PV) direct current (DC)²—

$$0 = I_{\text{ph}} - I_{\text{rs}} \left(e^{\frac{q(V+IR_s)}{N_s n k_B T}} - 1 \right) - G_p (V + IR_s) - I,$$


with auxiliary equations—

$$I_{\text{ph}} = I_{\text{rs}} \left(e^{\frac{qI_{\text{sc}}R_s}{N_s n k_B T}} - 1 \right) + G_p I_{\text{sc}} R_s + I_{\text{sc}},$$

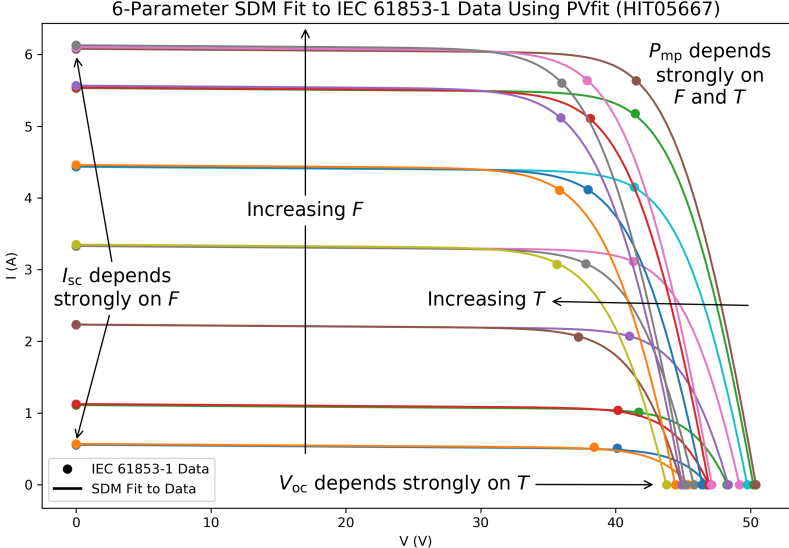
$$I_{\text{rs}} = I_{\text{rs}0} \left(\frac{T}{T_0} \right)^3 e^{\nu \frac{qE_{\text{g}0}}{nk_B} \left(\frac{1}{T_0} - \frac{1}{T} \right)},$$

$$n = n_0, \quad R_s = R_{s0}, \quad G_p = G_{p0}, \quad I_{\text{sc}} = F I_{\text{sc}0}.$$

“Irradiance” $F = \frac{I_{\text{sc}}}{I_{\text{sc}0}}$ and PV cell temperature T (junction).

²Current conservation under *homogeneity assumptions*. 

Performance w.r.t. Irradiance and Temperature



Parameter Inference (aka. Model Calibration)

Given sufficient measurements of observables—

$$V, I, T, \text{ and } F,$$

then infer six model parameters at reference condition (RC)—

$$I_{sc0}, I_{rs0}, n_0, R_{s0}, G_{p0}, \text{ and } E_{g0},$$

using a minimization-based solver with rescalings and careful choice of initial conditions—`scipy`'s `least_squares` (`dogbox`) or `odr`.

PVfit's formulation accommodates various measurement types. However—

- ▶ How do we work with F instead of traditional irradiance?
- ▶ Is “the” temperature given for PV cell(s), or back of module, or ambient, or ...?

Observing Irradiance and Temperature

- ▶ Calibration labs measure dense I-V curves using a PV reference device, where for each *point*—

$$F = \frac{I_{sc}}{I_{sc0}} = M \frac{I_{sc,ref}}{I_{sc,ref0}},$$

and the spectral correction M depends on the temperature-dependent spectral responsivity of *both* devices.

- ▶ IEC 61853-1 matrix provides several 3-point I-V curves (one at RC³), where for each *curve* with short-circuit current I_{sc} —

$$F = \frac{I_{sc}}{I_{sc0}}.$$

T is too loosely defined in IEC 61853-1 (my opinion).

Module and cell temperatures may, or may not, be close, e.g., continuous vs. flashed irradiance.

³Here, RC is the standard test condition (STC).

Performance Simulation (a.k.a. Model Prediction)

Given values of operating-condition (OC) observables—

$$F \text{ and } T,$$

then predict maximum power—

$$P_{\text{mp}} = I_{\text{mp}} \cdot V_{\text{mp}}.$$

However—

- ▶ F is traditionally observed using a reference device, with (mis)match depending on several conditions.
- ▶ T of the PV cell is rarely the observed temperature.

Using Meteorological (MET)-Station Data

Sandia Array Performance Model (SAPM) defines an effective irradiance, E_e —

$$E_e = \frac{I_{sc}}{I_{sc0} (1 + \alpha_{sc}(T - T_0))},$$

so that—

$$F = \frac{I_{sc}}{I_{sc0}} = E_e (1 + \alpha_{sc}(T - T_0)).$$

E_e (unitless) is readily calculated from MET-station data.⁴

⁴Technically, α_{sc} depends on spectrum of OC.

Calculation of Effective Irradiance

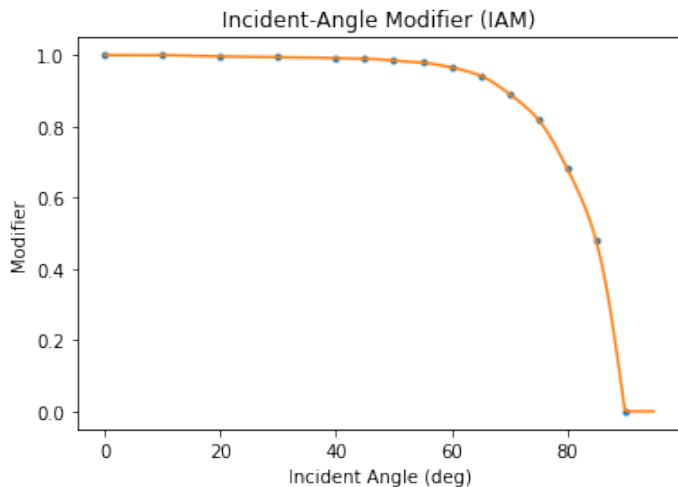
E_e is computed from plane-of-array (POA) irradiance, E_{POA} —

$$E_e = f_{\text{AM}_a} \frac{E_{\text{POA}}}{E_0} = f_{\text{AM}_a} \left(\frac{f_{\text{IAM}} E_b + f_d E_d}{E_0} \right).$$

- ▶ E_0 : irradiance at RC (1000 W/m² at STC)
- ▶ E_b : beam irradiance
- ▶ Incident angle modifier: $f_{\text{IAM}} = f_{\text{IAM}}(\text{AOI})$ — PCHIP⁵ of IEC 61853-2 data or physical model, with AOI from `pvlib`
- ▶ E_d : diffuse irradiance — sum of sky and ground components (e.g., isotropic and monthly albedo, respectively)
- ▶ Simple diffuse fraction model: $f_d = 1$ (non-concentrating)
- ▶ E_b and E_d from given GHI, DNI, and DHI using `pvlib`
- ▶ No absolute air-mass correction: $f_{\text{AM}_a} = 1$ (insufficient info)

Incident Angle Modifier

PCHIP is smooth, while respecting data's extrema.⁶



⁶Zero "tail" is separate.

Temperature from MET Data

Faiman model for module temperature, T_m , using POA irradiance, E_{POA} , ambient temperature, T_a , and wind speed, WS —

$$T_m = T_a \frac{E_{\text{POA}}}{U_0 + U_1 \cdot WS}.$$

T_m can be further transformed into cell temperature, T , using, e.g., SAPM—

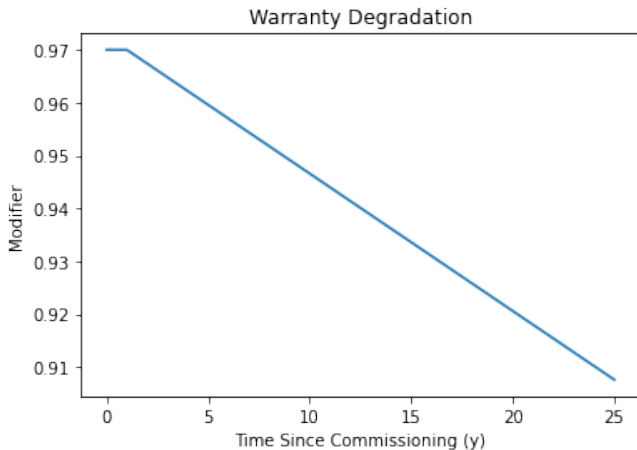
$$T = T_m + \frac{E_{\text{POA}}}{E_0} \Delta T.$$

U_0 , U_1 , and ΔT are installation- and module-dependent.⁷

⁷Because $F \approx \frac{E_{\text{POA}}}{E_0}$, one could recast models in terms of F .

Degradation and Other Losses

Warranty degradation using time since commissioning (worst case).



Soiling, mismatch, wiring, etc. not included (best case).

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Scenarios (1 of 2)

Considered three of six scenarios, omitting tracked and bifacial.

Albuquerque, NM, USA—

- 1: Panasonic 325W monofacial HIT, $N_s = 72$, 12 panels
- 2: Canadian Solar 275W monofacial mono-Si, $N_s = 60$, 12 panels

Roskilde, Denmark—

- 5: Trina Solar 305W monofacial mono-Si, $N_s = 60$, 88 panels

Scenarios (2 of 2)

For Panasonic & Canadian Solar in Albuquerque—

- ▶ IEC 61853-1 provided I-V matrix (assume $T = T_m$) and α_{sc}
- ▶ IEC 61853-2 measurements for U_0 , U_1 , and IAM

For Trina Solar in Roskilde—

- ▶ Datasheet had I_{sc} , I_{mp} , V_{mp} , & V_{oc} at STC & NOCT⁸ and α_{sc}
- ▶ U_0 and U_1 estimated, physical model for IAM

For all scenarios—

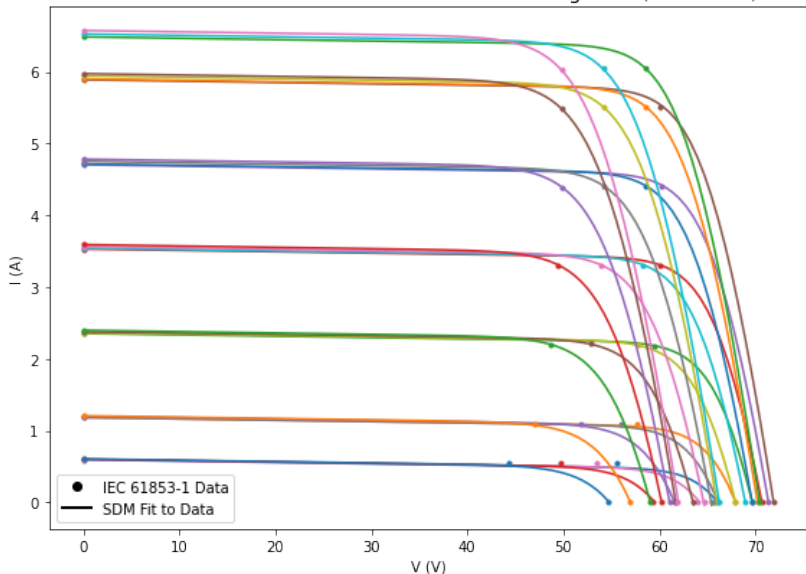
- ▶ Only Faiman temperature model ($\Delta T = 0$, not provided)

$$T = T_m + \frac{E_{POA} \Delta T}{E_0}$$

⁸Nominal operating cell temperature NOCT), *not* nominal module operating temperature (NMOT).

Panasonic 325W monofacial HIT (Albuquerque)

6-Parameter SDM Fit to IEC 61853-1 Data Using PVfit (Panasonic)



Panasonic 325W Monofacial HIT (Albuquerque)

Fit parameters (seconds to solve)—

I_{sc0}	I_{rs0}	n_0	R_{s0}	G_{p0}	E_{g0}
5.903 A	1.314e-12 A	1.304	0.7820 Ω	0.001893 S	1.575 eV

P_{mp} errors for model calibration ($\frac{P_{mp,fit} - P_{mp,meas}}{P_{mp,meas}}$, in %)—

	E_{POA} (W/m^2)						
T ($^{\circ}C$)	100	200	400	600	800	1000	1100
15	-10.0	-2.8	0.22	0.57	0.57	0.68	—
25	-9.1	-2.8	0.084	0.40	0.36	0.26	0.112
50	-8.1	-2.5	-0.21	0.28	0.188	-0.100	-0.30
75	-5.7	-0.86	0.61	0.41	0.24	-0.064	-0.183

Yearly PV-array energy from hourly powers: 134.841 kWh

Calculation of $F = I_{sc}/I_{sc0}$ (1 of 2)

I_{sc} (A) from IEC 61853-1 matrix—

T ($^{\circ}\text{C}$)	E_{POA} (W/m^2)						
	100	200	400	600	800	1000	1100
15	0.595	1.183	2.354	3.532	4.706	5.891	—
25	0.599	1.183	2.365	3.542	4.718	5.903	6.488
50	0.602	1.199	2.379	3.567	4.754	5.944	6.528
75	0.606	1.207	2.399	3.593	4.784	5.976	6.578

$I_{sc0} = 5.903$ A is in red — divisor for $F = \frac{I_{sc}}{I_{sc0}}$.

Calculation of $F = I_{sc}/I_{sc0}$ (2 of 2)

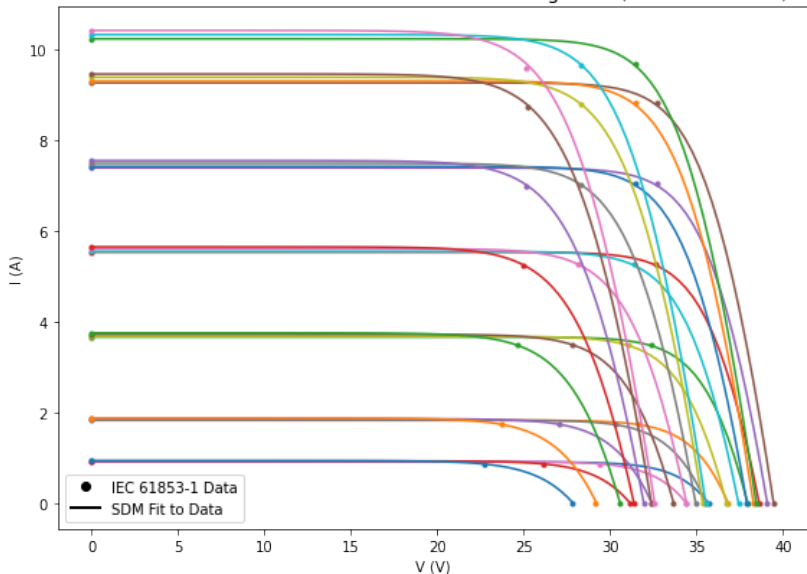
$F = \frac{I_{sc}}{I_{sc0}}$ from IEC 61853-1 matrix—

	E_{POA} (W/m^2)						
T ($^{\circ}C$)	100	200	400	600	800	1000	1100
15	0.1008	0.200	0.399	0.598	0.797	0.998	—
25	0.1015	0.200	0.401	0.600	0.799	1	1.099
50	0.1020	0.203	0.403	0.604	0.805	1.007	1.106
75	0.1026	0.204	0.406	0.609	0.810	1.0124	1.114

Shows that $F \neq \frac{E_{POA}}{E_0}$, merely $F \approx \frac{E_{POA}}{E_0}$.

Canadian Solar 275W Monofacial Mono-Si (Albuquerque)

6-Parameter SDM Fit to IEC 61853-1 Data Using PVfit (Canadian Solar)



Canadian Solar 275W Monofacial Mono-Si (Albuquerque)

Fit parameters (**minutes** to solve)—

I_{sc0}	I_{rs0}	n_0	R_{s0}	G_{p0}	E_{g0}
9.299 A	1.133e-09 A	1.088	0.2303 Ω	0.0 S	1.138 eV

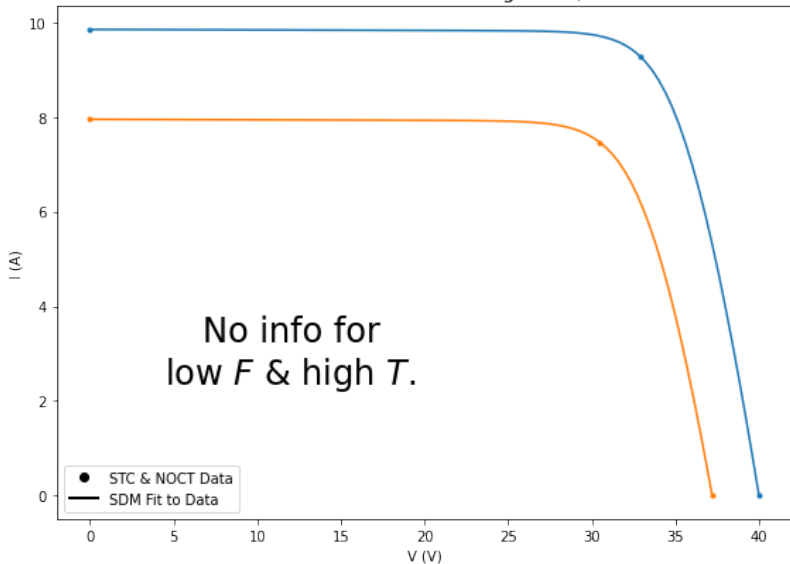
P_{mp} errors for model calibration ($\frac{P_{mp,fit} - P_{mp,meas}}{P_{mp,meas}}$, in %) —

	E_{POA} (W/m^2)						
T ($^{\circ}C$)	100	200	400	600	800	1000	1100
15	-0.70	-0.83	-0.97	-0.80	-0.69	-0.66	—
25	-0.166	-1.14	-0.88	-0.56	-0.42	-0.49	-0.50
50	0.110	-0.55	-0.30	-0.118	-0.0069	0.154	0.143
75	-0.34	-0.38	-0.118	0.37	0.51	0.72	0.85

Yearly PV-array energy from hourly powers: 114.361 kWh

Trina Solar 305W Monofacial Mono-Si (Roskilde)

6-Parameter SDM Fit to STC & NOCT Data Using PVfit (Trina Monofacial Fixed)



Trina Solar 305W Monofacial Mono-Si (Roskilde)

Fit parameters (seconds to solve)—

I_{sc0}	I_{rs0}	n_0	R_{s0}	G_{p0}	E_{g0}
9.85 A	3.488e-15 A	0.7299	0.3520 Ω	0.007732 S	1.272 eV

P_{mp} errors for model calibration ($\frac{P_{mp,fit} - P_{mp,meas}}{P_{mp,meas}}$, in %)—

	E_{POA} (W/m^2)	
T ($^{\circ}C$)	800	1000
25	–	0.077
44	0.039	–

CAUTION: Good fit does *not* guarantee good model!⁹

Yearly PV-array energy from hourly powers: 478.868 kWh

⁹This scenario's fit changed considerably when `scipy.odr` used instead.

Are We There Yet?

“All models are wrong, but some are useful.”

—George E. P. Box

- ▶ Key IEC 61853-1 measurement questions—
 - ▶ Module vs. cell temperature?
 - ▶ Matched reference device (spectral & angular response)?
 - ▶ Representative module sample? Variability estimates?
- ▶ Is complexity of PVsyst, double-diode model, ... worth it?
 - ▶ Photo-conductive shunt in SDM, e.g., $G_p = F \cdot G_{p0}$?
 - ▶ The FutureTM is bifacial, or perovskite, or ...?
- ▶ When do other factors swamp measurement & fitting errors?
 - ▶ $\Delta T = 0$ led to overestimated energy? (unblind hourly data)
 - ▶ 2–4% energy increase switching isotropic to haydavies!
 - ▶ Degradation, soiling, shading, mismatch, line losses, ...
 - ▶ Weather uncertainty, variability, availability, ...

Inter-comparisons needed to tease all this out...thank you PVPMC!

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Recasting the Inference Problem

Why not think/work directly in terms of F and T ?

Given a well-calibrated PV device with known parameters—

$$I_{sc0}, I_{rs0}, n_0, R_{s0}, G_{p0}, \text{ and } E_{g0},$$

and sufficient measurements of observables at one OC—

$$V \text{ and } I,$$

then infer the two model parameters—

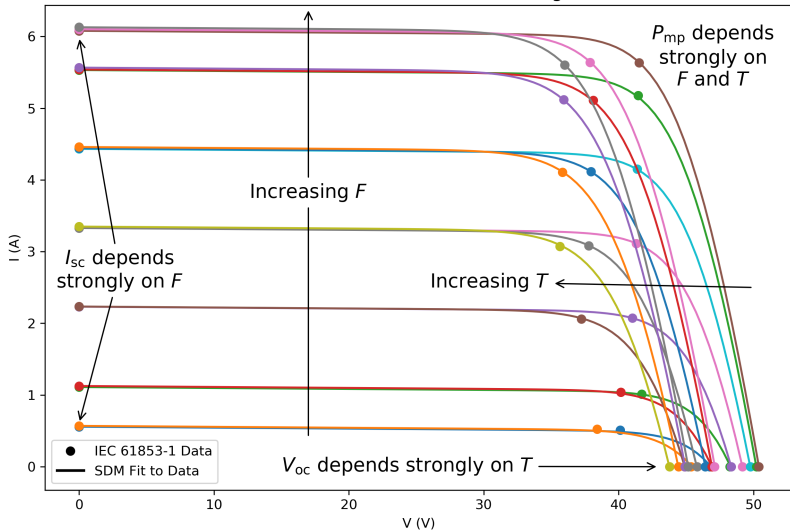
$$F \text{ and } T.$$

A minimally observed I-V curve could be simply I_{sc} and V_{oc} .¹⁰

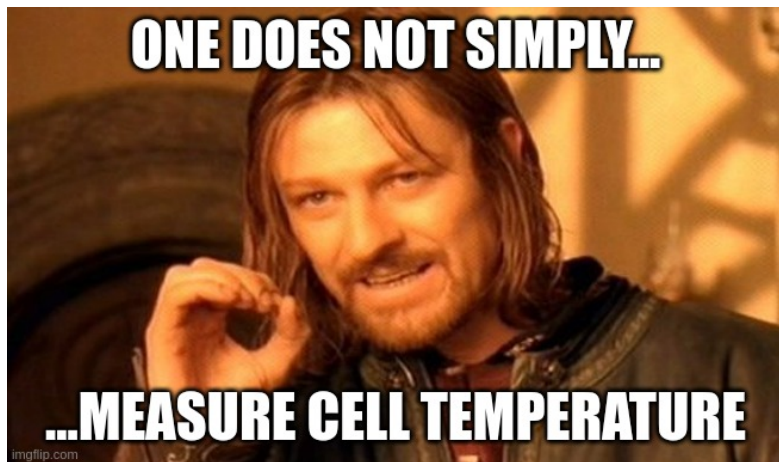
¹⁰Note absence of temperature-coefficients.

PV-Based Sensing of Irradiance and Cell Temperature

6-Parameter SDM Fit to IEC 61853-1 Data Using PVfit (HIT05667)



Rethinking Irradiance and Temperature (1 of 2)



Combine F and T with T_m measurements to infer ΔT !

Rethinking Irradiance and Temperature (2 of 2)

Soiling-measurement systems have matched reference devices—

- ▶ Simply (?) add V_{oc} measurement with I_{sc} to infer T
- ▶ Combine with T_m measurement (and F) to infer ΔT

$$T = T_m + \frac{E_{POA}}{E_0} \Delta T \approx T_m + F \cdot \Delta T$$



–Photo credit: NRGSystems

PVfit: Because Measurements Cost Money

Model calibration at <https://pvfit.app> or via REST API

PVfit

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PVfit: Single Diode Model (SDM)

FIT INFO API

SDM Calibration over a Range of Irradiance and Temperature

Input: I-V Curve Data

[LOAD EXAMPLE DATA](#) 60-cell mono x-Si module 72-cell poly x-Si module 216-cell CdTe module

I-V-F-T Curves IEC 61853-1 Matrix

Input IEC 61853-1 matrix data, then click COMPUTE FIT (standard test conditions (STC) are 1000 W/m² and 25°C, with grey cells optional)

Irradiance (W/m ²) @ AM 1.5	Module Temperature (°C)							
	15		25		50		75	
1100	<u>I_{sc} (A)</u>	<u>P_{mp} (W)</u>	<u>I_{sc} (A)*</u>	<u>P_{mp} (W)*</u>	<u>I_{sc} (A)*</u>	<u>P_{mp} (W)*</u>	<u>I_{sc} (A)*</u>	<u>P_{mp} (W)*</u>
	<u>V_{mp} (V)</u>	<u>V_{oc} (V)</u>	<u>V_{mp} (V)*</u>	<u>V_{oc} (V)*</u>	<u>V_{mp} (V)*</u>	<u>V_{oc} (V)*</u>	<u>V_{mp} (V)*</u>	<u>V_{oc} (V)*</u>
1000	<u>I_{sc} (A)*</u>	<u>P_{mp} (W)*</u>	<u>I_{sc} (A)*</u>	<u>P_{mp} (W)*</u>	<u>I_{sc} (A)*</u>	<u>P_{mp} (W)*</u>	<u>I_{sc} (A)*</u>	<u>P_{mp} (W)*</u>

1.1.1 © 2022, [Intelligent Measurement Systems LLC](#)

Open-source simulation code at
<https://github.com/markcampanelli/pvfit>

References

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2. *pvlib-python*, <https://github.com/pvlib/pvlib-python>
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